

Class 10-Mathematics

Instructions for students: The notes provided must be copied to the Maths copy and then do the homework in the same copy.

Chapter 17

MENSURATION (Part - 6)

CONVERSION OF SOLID FROM ONE SHAPE TO ANOTHER

When a solid is converted from one shape to another, its volume remains same, but the surface area changes.

Exercise 17.5

5. Radius of cylindrical vessel = 1 m
Height of cylindrical vessel = 3.5 m
Volume of water = Volume of cylindrical vessel
= $\pi r^2 h$
= $\frac{22}{7} \times 1 \times 3.5$
= 11 m^3
Height of water on roof = $\frac{\text{Volume of water}}{\text{Length} \times \text{breadth}}$
= $\frac{11}{22 \times 20} = \frac{1}{40} \text{ m} = \frac{10}{4} \text{ cm} = 2.5 \text{ cm}$
Rain fall = 2.5 cm

8. Radius of the metallic disk = 12 cm
Height = $2.5 \text{ mm} = .25 \text{ cm} = \frac{1}{4} \text{ cm}$
Volume = $\pi r^2 h$
= $\pi \times 144 \times \frac{1}{4} = 36\pi$
Volume of sphere = $\frac{4}{3} \pi r^3$
Volume of sphere = Volume of disc (Cylinder)
 $\frac{4}{3} \pi r^3 = 36\pi$
 $r^3 = 36 \times \frac{3}{4}$

$$= 27$$

$$\text{Radius of sphere, } r = \sqrt[3]{27} = 3 \text{ cm}$$

12. Internal radius of metallic cylindrical tube, $r = 3 \text{ cm}$

$$\text{Thickness} = \frac{1}{2} \text{ cm} = .5 \text{ cm}$$

$$\text{External radius, } R = 3.5 \text{ cm}$$

$$\text{Height, } h = 21 \text{ cm.}$$

$$\begin{aligned} \text{Volume} &= \pi(R^2 - r^2)h \\ &= \pi((3.5)^2 - 3^2)21 \\ &= \pi(12.25 - 3) \times 21 \\ &= \pi \times 3.25 \times 21 \end{aligned}$$

$$\text{Height of the cone made} = 7 \text{ cm}$$

$$\text{Radius} = ?$$

$$\begin{aligned} \text{Volume of cone} &= \frac{1}{3} \pi r^2 h \\ &= \frac{1}{3} \times \pi \times r^2 \times 7 \end{aligned}$$

$$\text{Volume of cone} = \text{Volume of tube}$$

$$\frac{1}{3} \times \pi \times r^2 \times 7 = \pi \times 3.25 \times 21$$

$$r^2 = \frac{3.25 \times 21 \times 3}{7}$$

$$= 3.25 \times 9 = 29.25$$

$$r = \sqrt{29.25}$$

$$= 5.4 \text{ cm approx.}$$

Home Work: Solve Exercise **17.5** questions 1 to 15 in the Maths copy.